

# The Thinner Takes It All

Applications of thinned point processes in ecology

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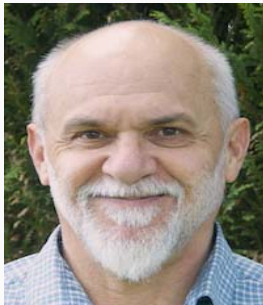
Andy Seaton

University of St Andrews

# Acknowledgements



**Dr Janine Illian,**  
University of St Andrews



**Prof David Borchers,**  
University of St Andrews



**Prof Finn Lindgren,**  
University of Edinburgh

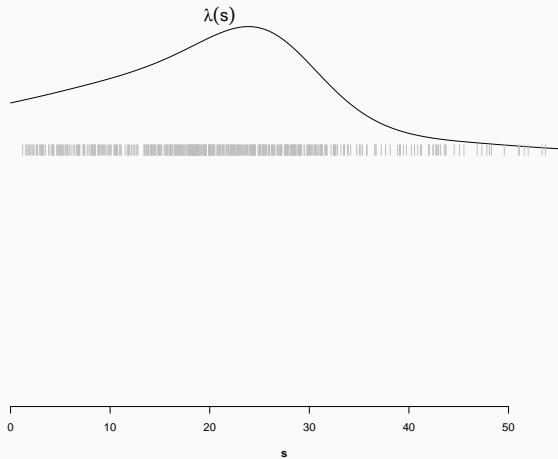
**Dr Fabian Bachl, University of Edinburgh**

**Rick Camp, University of St Andrews and US Geological Survey**

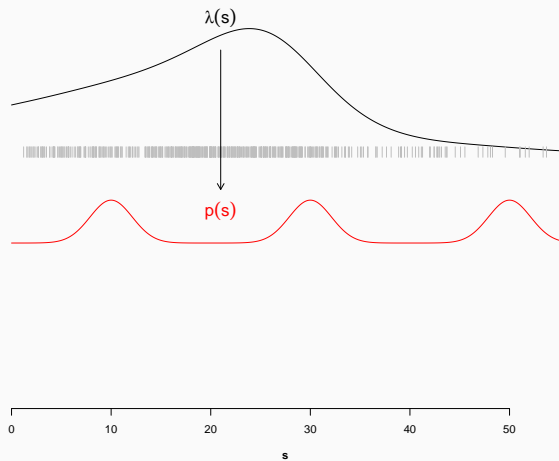
**Dr David Miller, University of St Andrews**

1. Distance Sampling and “Density Surface” Models
2. Spatial Capture-Recapture

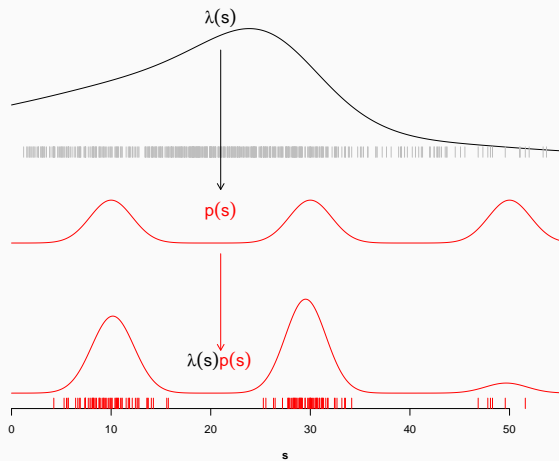
# Thinned Poisson Processes



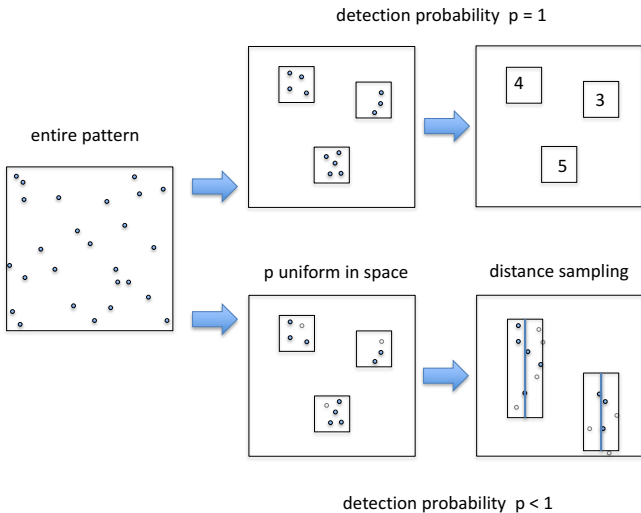
# Thinned Poisson Processes



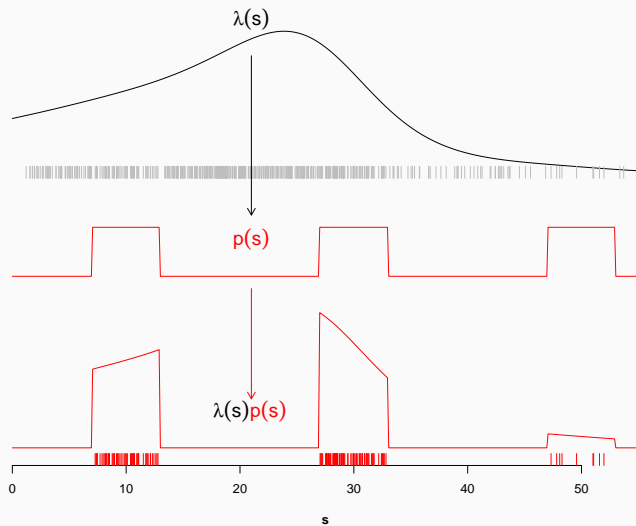
# Thinned Poisson Processes



# Distance Sampling

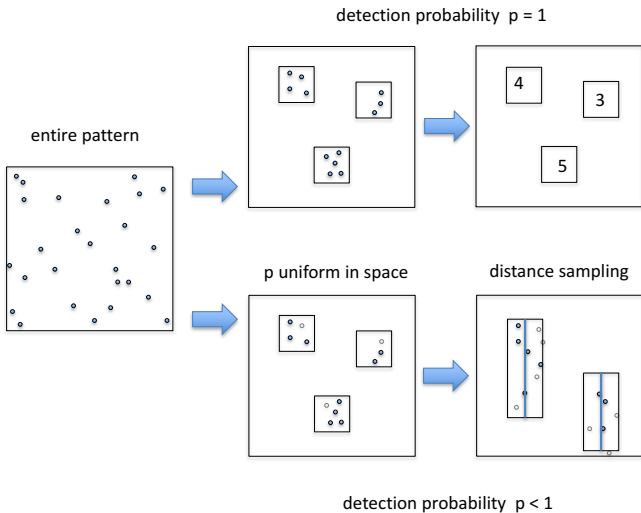


# Distance Sampling

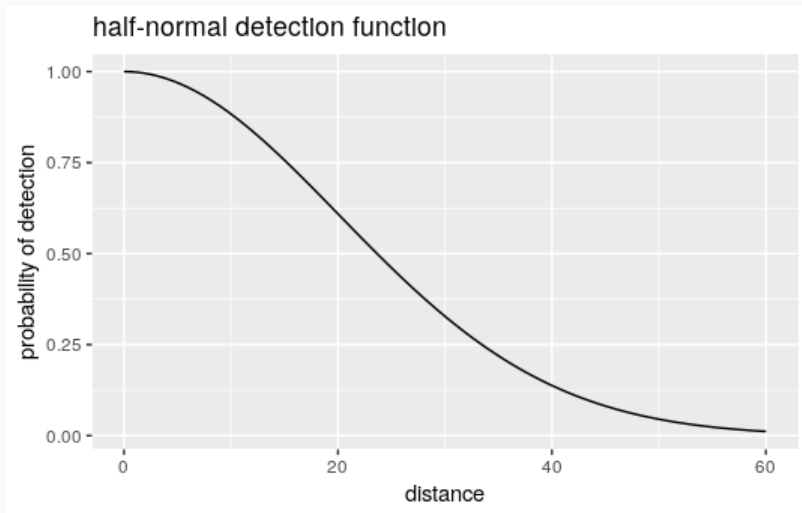




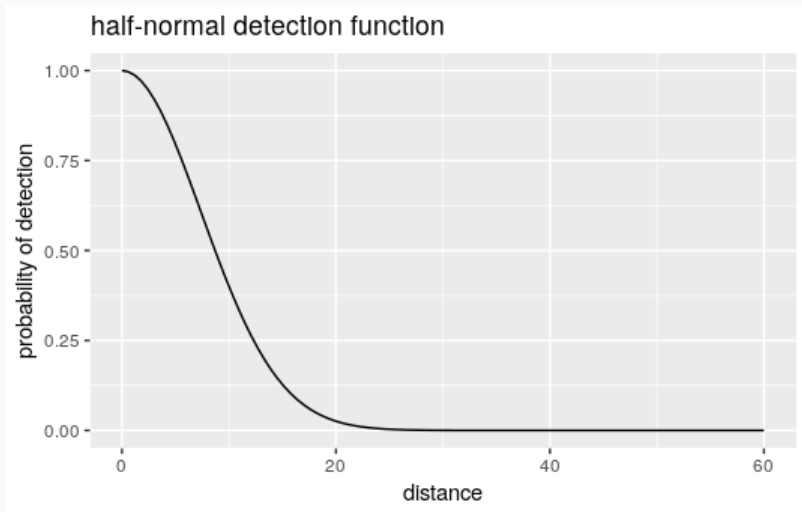
# Distance Sampling



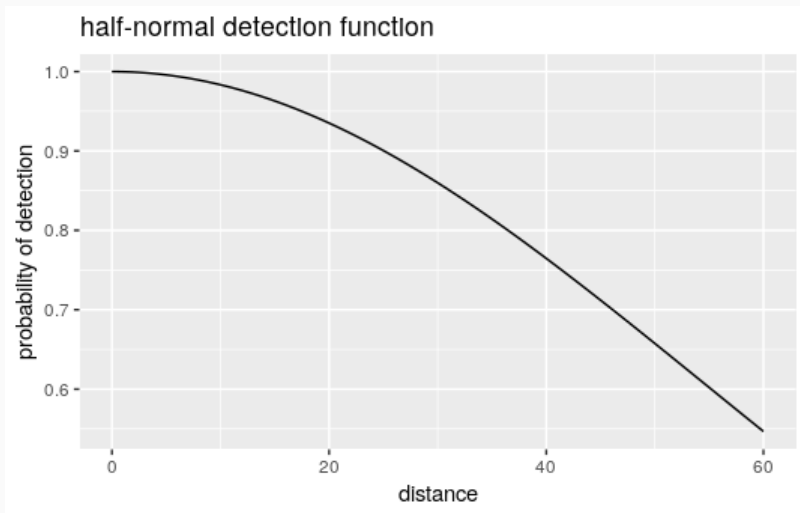
## Distance Sampling - the detection function



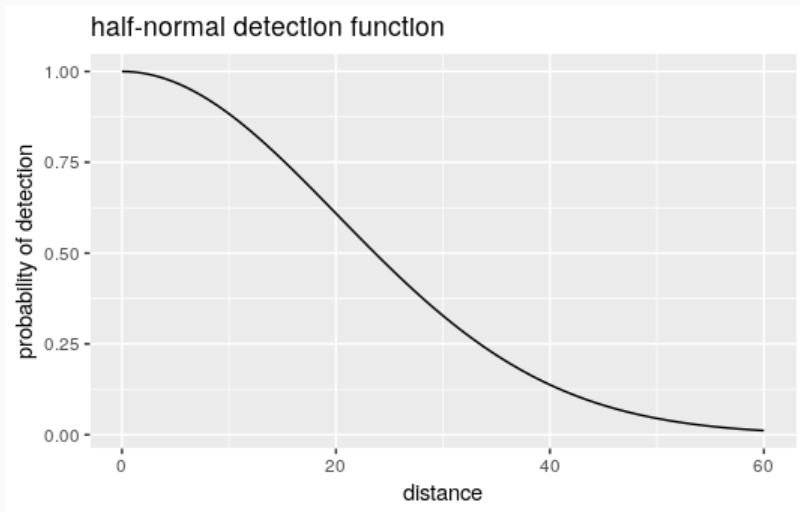
## Distance Sampling - the detection function



## Distance Sampling - the detection function



## Distance Sampling - the detection function



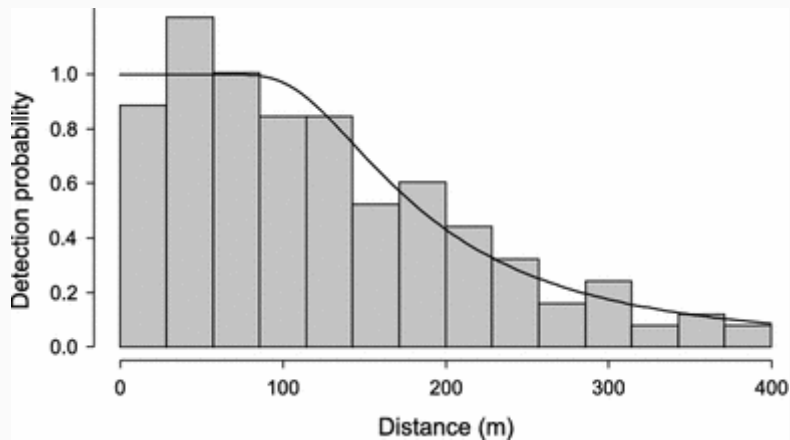
Note the intercept assumed equal to 1

## Distance Sampling - the detection function

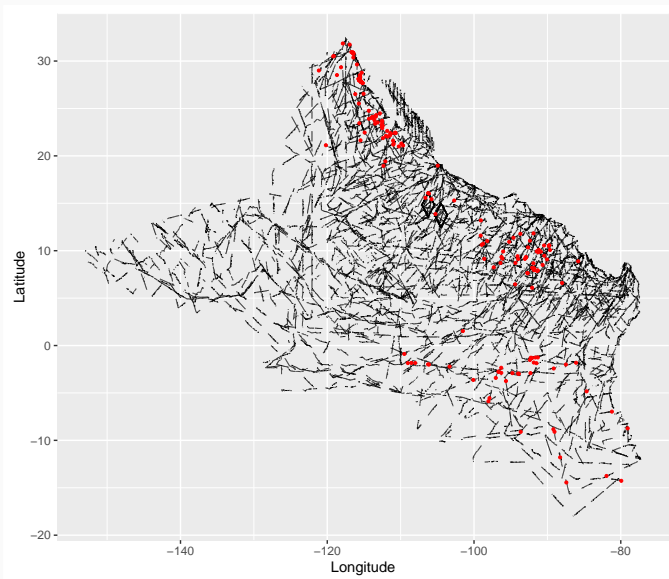


source: [the birdist.com](http://thebirdist.com)

## Distance Sampling - the detection function

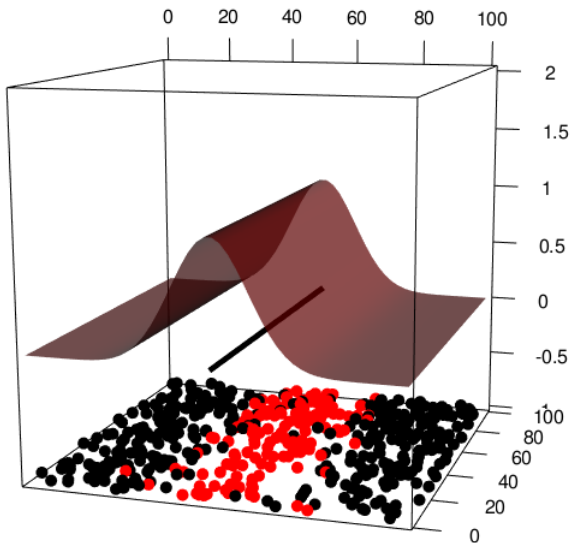


# Line transect example - whale survey

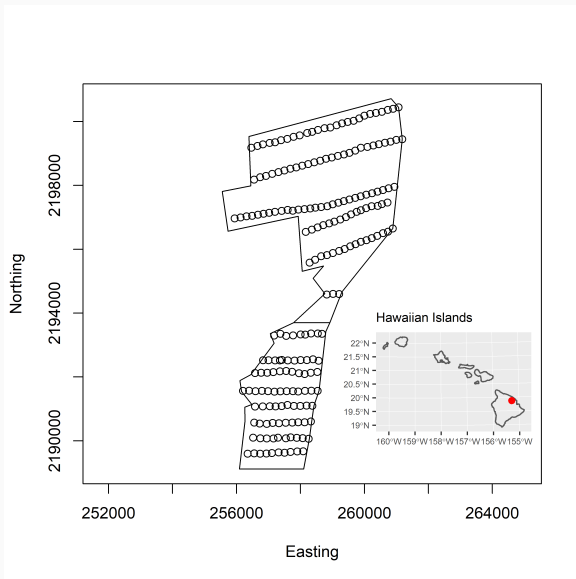




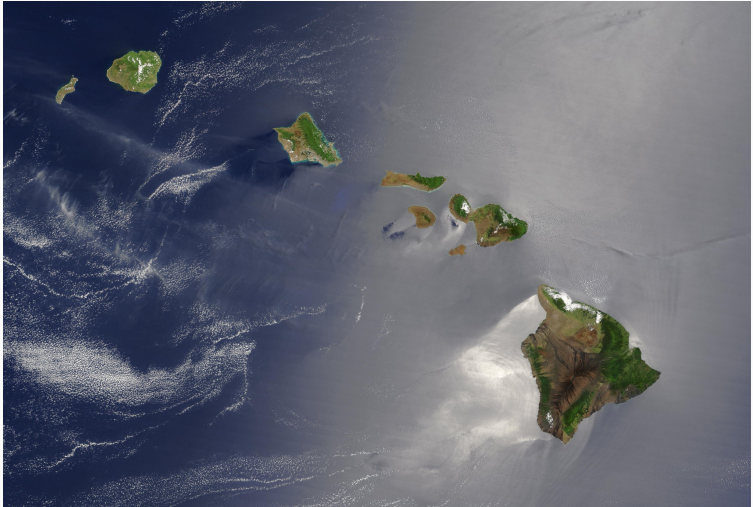
## Line transect example - whale survey



# Point transect example - Hawaiian Akepa survey



# Point transect example - Hawaiian Akepa survey



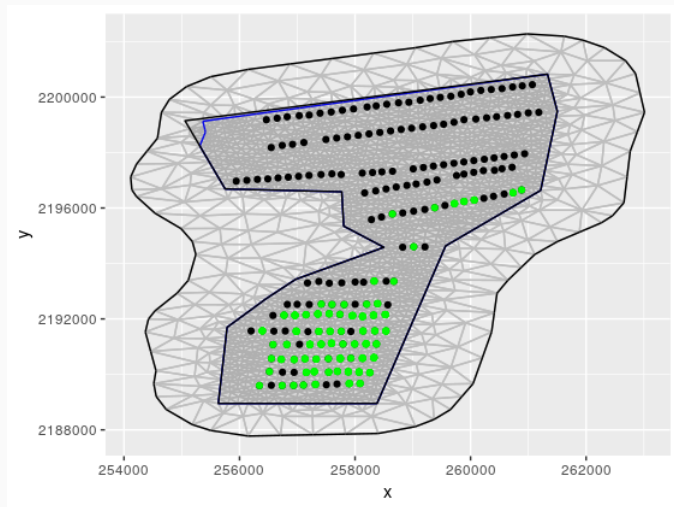
source: wikicommons

## Point transect example - Hawaiian Akepa survey

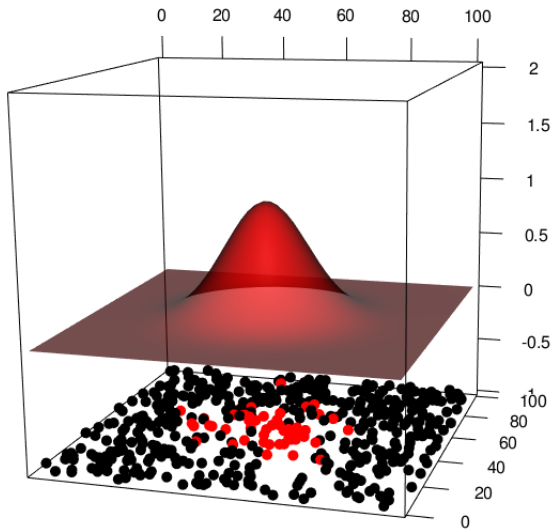


source: Jack Jeffrey, US Fish and Wildlife Service

# Point transect example - Hawaiian Akepa survey



## Point transect example - Hawaiian Akepa survey



## Point transect example

Recall that the intensity for detected points is  $\tilde{\lambda}(s) = \lambda(s)p(s)$

Therefore,

$$\log \tilde{\lambda}(s) = \log \lambda(s) + \log p(s)$$

But  $\log p(s)$  is typically not linear in its parameters! (e.g. half-normal requires strictly positive variance parameter)

Solution: iterated INLA

## Point transect example - iterated INLA

inlabru syntax example:

```
thinning = function(distance, log_sigma){
  exp(-distance^2 / 2 exp(log_sigma)^2)
}

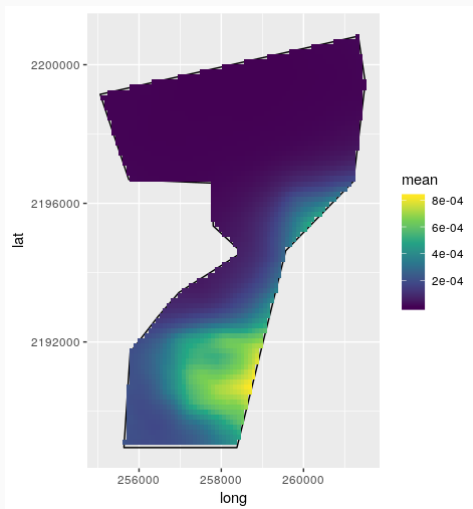
formula = coordinates + distance ~
  Intercept + ... + log(thinning(distance, log_sigma))

components = ~ Intercept + ... + log_sigma

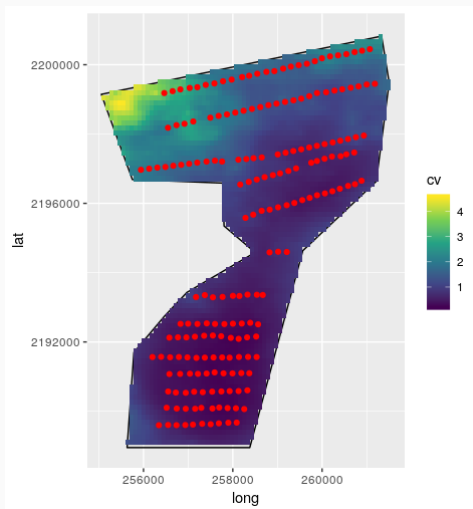
lgcp(components, # tell lgcp what are parameters to be estimated
  data, # data as sp object
  formula, # tell lgcp how to construct the linear predictor
  samplers) # sampling locations as sp object
```



# Point transect example - Hawaiian Akepa survey



# Point transect example - Hawaiian Akepa survey



## Point transect example - Hawaiian Akepa survey

A slight problem: we did not know the exact location of the point, only the distance from the observer.

Solution: derive the appropriate intensity for this partial data

## Point transect example - Hawaiian Akepa survey

For a single point transect at location  $\mathbf{s}_0$ , letting  $\mathbf{s}(r, \theta) = \mathbf{s}_0 + r[\cos \theta, \sin \theta]^T$ , the intensity for points at distance  $r$  from  $\mathbf{s}_0$  is:

$$\begin{aligned}\tilde{\lambda}(r) &= \int_{c(r)} \lambda(\mathbf{s}(r, \theta)) p(r) d\mathbf{s} \\ &= \int_0^{2\pi} r \lambda(\mathbf{s}(r, \theta)) p(r) d\theta \\ &= 2\pi r \lambda(\mathbf{s}_0) p(r)\end{aligned}$$

Add a  $\log(2\pi)$  offset for not knowing  $\theta$  and a  $\log r$  offset to account for the fact that we consider a larger area with increasing distance.

## Point transect example - take home messages

- Conceptually nice one-stage model - avoids binning points into counts and uncertainty propagation between two stages
- Intensities can be derived for data even where you cannot draw a point on a map (more on this next)
- Iterated INLA a general tool for more than just fitting a thinning probability function

# Spatial Capture-Recapture

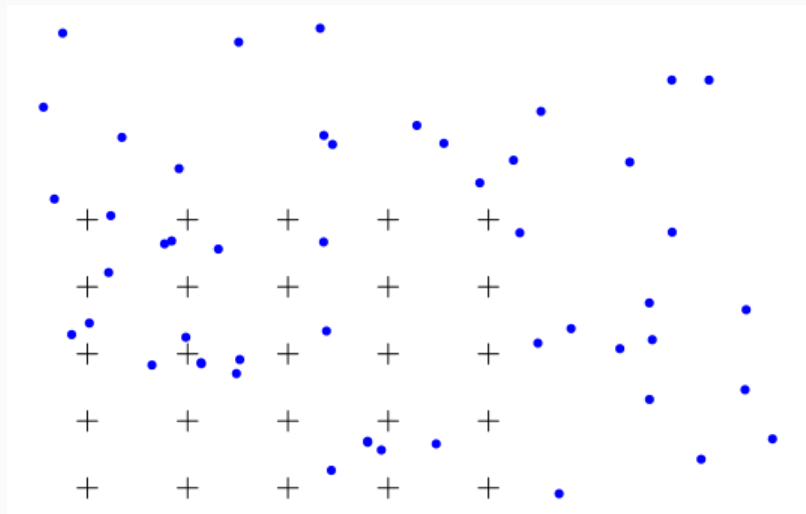
- capture-recapture methods have a long history of being used to estimate the size of a population
- **spatial** capture-recapture uses the location information of captures and recaptures
- a natural way to join capture-recapture data and spatial modelling

# Spatial Capture-Recapture



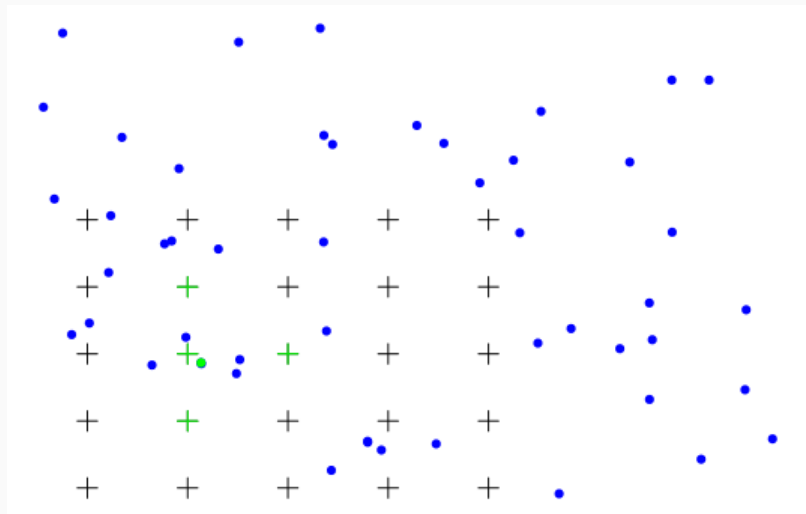
source: snow leopard conservancy trust

# Spatial Capture-Recapture

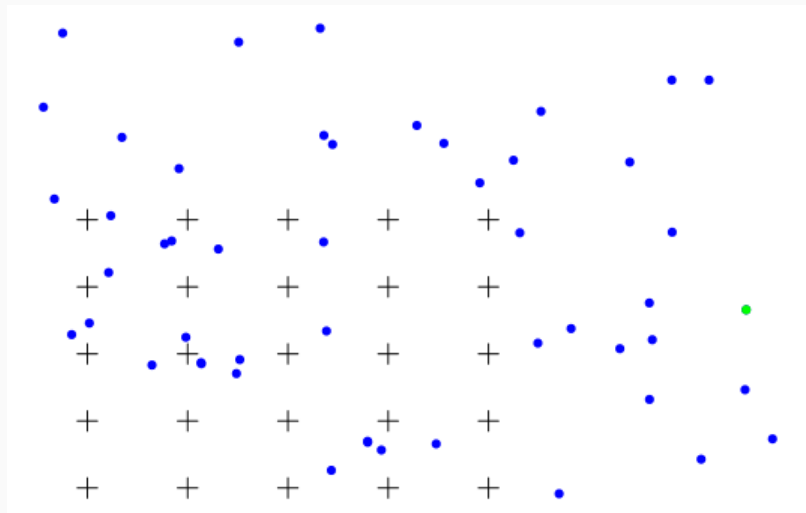




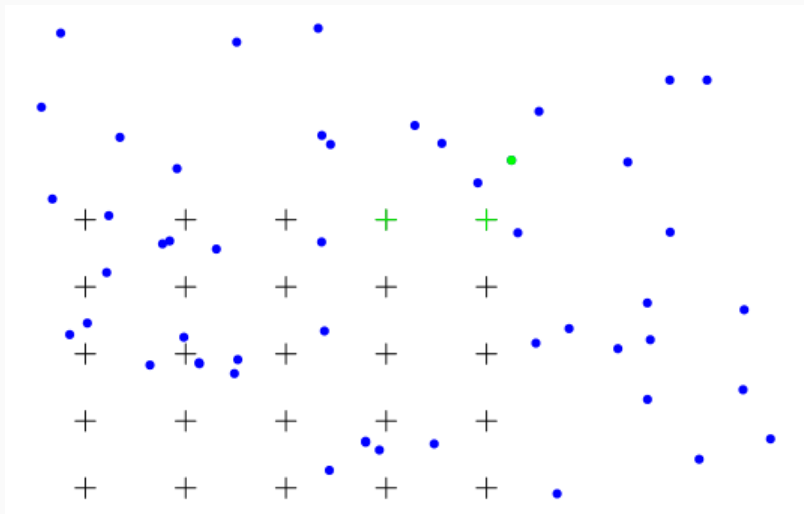
# Spatial Capture-Recapture



# Spatial Capture-Recapture



# Spatial Capture-Recapture



## Spatial Capture-Recapture - the likelihood

$$\mathcal{L}(\Omega) \propto \exp\left(-\int \lambda(\mathbf{s})p(\mathbf{s}|\phi)d\mathbf{s}\right) \prod_{i=1}^n \int \pi(\Omega_i|\phi, \mathbf{s}_i)\lambda(\mathbf{s}_i)d\mathbf{s}_i$$

- The thinning and the estimation of the activity centre location share parameters  $\phi$
- Inference usually maximum-likelihood or Bayesian approach in MCMC
- Typically  $\lambda(\mathbf{s})$  is assumed constant or linear combination of fixed effect covariates
- Watch this space for  $\lambda(\mathbf{s})$  a realisation of log-Gaussian Cox process...

# Summary

- Thinning functions are a natural way to account for how ecologists observe point patterns
- Complex observation processes can be represented as a thinning - conditioning on auxiliary data (such as distances and other covariates) or being derived from a more complicated observation model (as in SCR)
- General software for specifying thinning functions has the potential to be widely used
- Potential for thinning to share information between for multiple observation processes e.g. citizen science, combining multiple data sources etc

Thanks for listening!